

A NOTE ON MATRIX VERSIONS OF KANTOROVICH–TYPE INEQUALITY

FEIXIANG CHEN

Abstract. Some new matrix versions of Kantorovich-Type inequalities for Hermitian matrix are proposed in this paper. We consider what happens to these inequalities when the positive definite matrix is allowed to be positive semidefinite singular or indefinite.

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