

THE STEINER SYMMETRIZATION OF LOG-CONCAVE FUNCTIONS AND ITS APPLICATIONS

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Abstract. In this paper, we give a new definition of functional Steiner symmetrizations on log-concave functions. Using the functional Steiner symmetrization, we give a new proof of the classical Prékopa-Leindler inequality on log-concave functions.

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