

EQUIVALENCE OF SOME MATRIX INEQUALITIES

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Abstract. In the present article, some Kantorovich type and Wielandt type matrix inequalities and their equivalent forms are discussed respectively, and the equivalence of these Kantorovich type inequalities with the corresponding Wielandt type inequalities are established too.

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