

SOME DYNAMIC HARDY-TYPE INEQUALITIES WITH GENERAL KERNEL

MARTIN BOHNER, AMMARA NOSHEEN, JOSIP PEČARIĆ AND AWAIS YOUNUS

Abstract. In this paper, we extend some Hardy-type inequalities with certain kernels to arbitrary time scales. Certain classical and some new integral and discrete inequalities are deduced in seek of applications.

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