

PROPERTIES OF THE SYMBOL OF MULTIDIMENSIONAL SINGULAR INTEGRALS IN THE WEIGHTED SPACES AND OSCILLATING MULTIPLIERS

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Abstract. Differential properties of symbols of multidimensional singular integrals in the weighted space of Bessel potentials on the sphere with the weighted functions, having singularities on a sphere are studied. The main results are applied to obtaining theorems on Fourier multipliers of spherical harmonic expansions.

Mathematics subject classification (2010): 42B15, 42B25, 42B35.

Keywords and phrases: Symbols, Beltrami operator, spherical harmonics, Hardy inequalities, multipliers, the space of potentials.

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