

A MULTIDIMENSIONAL DISCRETE HILBERT–TYPE INEQUALITY

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Abstract. In this paper, by using the way of weight coefficients and technique of real analysis, a multidimensional discrete Hilbert-type inequality with parameters and a best possible constant factor is given. The equivalent form, the operator expressions with the norm are also considered.

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