

n -EXPONENTIAL CONVEXITY OF SOME DYNAMIC HARDY-TYPE FUNCTIONALS

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Abstract. Recently, some dynamic Hardy-type inequalities with certain kernels are studied in [5] with the help of arbitrary time scales. We use the positive linear functionals obtained from the results of [5] to give non trivial examples of n -exponentially convex functions.

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