

SOME INEQUALITIES FOR EDGE LENGTHS AND CIRCUM-RADIUS OF A SIMPLEX IN HYPERBOLIC SPACE

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Abstract. For an n -dimensional simplex in hyperbolic space $H_n(-1)$ and spherical space $S_n(1)$, we establish some inequalities for its edge lengths and circum-radius.

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