

**BOUNDEDNESS ON MORREY SPACE FOR TOEPLITZ
TYPE OPERATOR ASSOCIATED TO SINGULAR INTEGRAL
OPERATOR WITH VARIABLE CALDERÓN–ZYGmund KERNEL**

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Abstract. In this paper, the boundedness of the Toeplitz type operators associated to the singular integral operator with variable Calderón-Zygmund kernel on Morrey spaces is obtained. For this purpose, some M^{λ} -type sharp maximal function inequalities for the operators are proved.

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