

## BOUNDEDNESS ON MORREY SPACE FOR TOEPLITZ TYPE OPERATOR ASSOCIATED TO SINGULAR INTEGRAL OPERATOR WITH VARIABLE CALDERÓN-ZYGMUND KERNEL

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**Abstract.** In this paper, the boundedness of the Toeplitz type operators associated to the singular integral operator with variable Calderón-Zygmund kernel on Morrey spaces is obtained. For this purpose, some  $M^k$ -type sharp maximal function inequalities for the operators are proved.

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