

UNCERTAINTY PRINCIPLE FOR THE SPHERICAL MEAN OPERATOR

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Abstract. The $L^p - L^q$ version of Miyachi's theorem is proved for the Fourier transform associated with the spherical mean operator.

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