

SOME BMO ESTIMATES FOR VECTOR-VALUED MULTILINEAR OPERATORS

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Abstract. In this paper, some *BMO* endpoint estimates for certain multilinear integral operators are obtained. The operators include Littlewood-Paley operator, Marcinkiewicz operator and Bochner-Riesz operator.

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