

ON THE RANGE OF THE PARAMETERS FOR THE GRAND FURUTA INEQUALITY TO BE VALID II

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Abstract. We will investigate the range of the parameters which make the grand Furuta inequality valid.

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