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LYAPUNOV–TYPE INEQUALITIES FOR HIGHER–ORDER DIFFERENTIAL EQUATIONS WITH ONE–DIMENSIONAL p–LAPLACIAN

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Abstract. In this paper, we establish Lyapunov-type inequalities for a single higher-order differential equation, a cycled system and a coupled system with one-dimensional p-Laplacian. Our result generalize some given results.

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