

OPERATOR INEQUALITIES INVOLVING THE ARITHMETIC, GEOMETRIC, HEINZ AND HERON MEANS

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Abstract. In this paper we present two improved arithmetic-geometric inequalities with Kantorovich constant (Lemma 3 and Lemma 5), based on which we provide some refinements in the operator case and then finally refer to the operator inequalities involving Heinz and Heron means.

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