

DIFFERENTIAL HARNACK INEQUALITY FOR NONLINEAR HEAT EQUATIONS

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Abstract. In this paper, we establish some differential Harnack inequalities for positive solutions to nonlinear heat equations coupled with the Bernhard List's flow. We also give some applications of these inequalities.

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