CERTAIN L^p BOUNDS FOR ROUGH SINGULAR INTEGRALS

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Abstract. In this paper, we prove L^p bounds for singular integrals with rough kernels associated to certain surfaces. Our results extend as well as improve previously obtained results.

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