

GENERALIZATION OF HUA'S INEQUALITIES AND AN APPLICATION

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Abstract. We generalize a new Hua's inequality and apply it to proof the boundedness of composition operator C_ϕ from p -Bloch space $\beta^p(Y_l(N, m, n; K))$ to q -Bloch space $\beta^q(Y_l(N, m, n; K))$ in this paper, where $Y_l(N, m, n; K)$ denotes the first Cartan-Hartogs domain, and $p \geq 0$, $q \geq 0$.

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