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HÖLDER AND MINKOWSKI TYPE INEQUALITIES WITH ALTERNATING SIGNS

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Abstract. We obtain new inequalities with alternating signs of Hölder and Minkowski type.

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