INEQUALITIES FOR THE MIXED DISCRIMINANTS

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Abstract. In the paper, some new inequalities for the mixed discriminants are established, which are the matrix analogues of inequalities of the well-known mixed volumes function.

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