

GENERALIZED COMPOSITION OPERATORS FROM ZYGMUND TYPE SPACES TO Q_K SPACES

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Abstract. Let φ be an analytic self-map of \mathbb{D} and $g \in H(\mathbb{D})$. The boundedness and compactness of generalized composition operators

$$(C_{\varphi}^g f)(z) = \int_0^z f'(\varphi(\xi))g(\xi)d\xi, \quad z \in \mathbb{D}, \quad f \in H(\mathbb{D})$$

from Zygmund type spaces to Q_K spaces are investigated.

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