

A FUNCTIONAL GENERALIZATION OF DIAMOND- α INTEGRAL MINKOWSKI'S TYPE INEQUALITY ON TIME SCALES

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Abstract. In this paper, we establish a functional generalization of Minkowski's type inequality on time scales based on diamond- α integral, which is introduced as a linear combination of the delta and nabla integrals. Some related results are also obtained.

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