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GENERALIZED STEFFENSEN'S INEQUALITY

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Abstract. We give a generalization of Steffensen's inequality by extending the results of Pečarić [4] and Rabier [5]. We make use of the n-order Taylor expansion of a composition of functions and Faà di Bruno's formula for higher order derivatives of the composition.

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