IMPROVEMENTS OF THE HERMITE–HADAMARD INEQUALITY ON TIME SCALES

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Abstract. In this paper we give refinements of converse Jensen's inequality as well as of the Hermite-Hadamard inequality on time scales. We give mean value theorems and investigate logarithmic and exponential convexity of the linear functionals related to the obtained refinements. We also give several examples which illustrate possible applications for our results.

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