

NEW RESULTS ABOUT HARDY-TYPE INEQUALITY

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Abstract. We give a Levinson type generalization of Hardy's inequality with convex functions replaced by 3-convex functions at a point. Several results and examples are provided, both one-dimensional and multidimensional.

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