

SOME SHARP INEQUALITIES ON MIXED-NORM SPACES ON THE UNIT BALL

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Abstract. We give some sharp inequalities on the mixed-norm spaces of holomorphic and harmonic functions on the unit balls in \mathbb{C}^n and \mathbb{R}^n respectively. Several interesting corollaries and applications of the inequalities are also given.

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