

EXTENSIONS OF THE HERMITE–HADAMARD INEQUALITY FOR CONVEX FUNCTIONS VIA FRACTIONAL INTEGRALS

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Abstract. The main aim of this paper is to give extension and refinement of the Hermite–Hadamard inequality for convex functions via Riemann–Liouville fractional integrals. We show how to relax the convexity property of the function f . Obtained results in this work involve a larger class of functions.

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