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COEFFICIENT ESTIMATES OF NEW CLASSES OF q–STARLIKE AND q–CONVEX FUNCTIONS OF COMPLEX ORDER

T. M. SEOUDY AND M. K. AOUF

Abstract. We introduce new classes of q-starlike and q-convex functions of complex order involving the q-derivative operator defined in the open unit disc. Furthermore, we find estimates on the coefficients for second and third coefficients of these classes.

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