

A REFINEMENT OF THE DIFFERENCE BETWEEN TWO INTEGRAL MEANS IN TERMS OF THE CUMULATIVE VARIATION AND APPLICATIONS

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Abstract. In this paper, we establish a refinement of the difference between two integral means for functions of bounded variation in terms of the cumulative variation function. The applications for probability density functions are also given.

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