𝒟–MEASURABILITY AND t–WRIGHT CONVEX FUNCTIONS

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Abstract. In the paper we will prove that each t-Wright convex function, which is bounded on a $\mathscr{D}$-measurable non-Haar meager set is continuous. Our paper refers to papers [11], [4] and a problem posed by K. Baron and R. Ger.

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