

THE GENERALIZED TSALLIS RELATIVE OPERATOR ENTROPY VIA SOLIDARITY

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Abstract. In this paper, some operator inequalities related to the solidarity and the generalized Tsallis relative operator entropy are shown. As an application, we show the Shannon type operator inequalities and its reverse in terms of the generalized Tsallis relative operator entropy.

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