NEW WEIGHTED ČEBYŠEV–OSTROWSKI TYPE
INTEGRAL INEQUALITIES ON TIME SCALES

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Abstract. In this paper we obtain some weighted Čebyšev-Ostrowski type integral inequalities on time scales involving functions whose first derivatives belong to $L_p(a,b)$ $(1 \leqslant p \leqslant \infty)$. We also give some other interesting inequalities as special cases.

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