

SOME INEQUALITIES ON THE PERRON EIGENVALUE AND EIGENVECTORS FOR POSITIVE TENSORS

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Abstract. In this paper, we obtain new bounds for the maximal eigenvalue and eigenvectors of positive tensors and compare these bounds with the known bounds. Numerical experiments are given to validate the efficiency of our new bounds.

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