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AN INEQUALITY FOR INTEGRALS OF THE FORM $\int_x^\infty f(t)e^{it}\,dt$

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Abstract. It is shown that for a completely monotonic function f, the absolute value of $\int_x^\infty f(t)e^{it}\,dt$ is not greater than $f(x)$.

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