

## NEW INEQUALITIES OF THE HERMITE–HADAMARD TYPE FOR $n$ -TIME DIFFERENTIABLE FUNCTIONS WHICH ARE QUASICONVEX

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*Abstract.* In this paper, by using an integral identity and the Hölder integral inequality we establish several new inequalities for  $n$ -time differentiable mappings that are connected with the Hermite-Hadamard inequality.

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