

HEISENBERG UNCERTAINTY INEQUALITY FOR GABOR TRANSFORM

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Abstract. We discuss the Heisenberg uncertainty inequality for groups of the form $K \rtimes \mathbb{R}^n$, K is a separable unimodular locally compact group of type I. This inequality is also proved for Gabor transform for several classes of groups of the form $K \rtimes \mathbb{R}^n$.

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