

GENERALIZED OPIAL—TYPE INEQUALITIES FOR DIFFERENTIAL AND INTEGRAL OPERATORS WITH SPECIAL KERNELS IN FRACTIONAL CALCULUS

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Abstract. In this paper we give Opial–type inequalities for two functions and multiple Opial–type inequalities by using generalized fractional differential and integral operators with special kernels. Also, we deduce some results that already have been proved in [9, 10].

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