

A NOTE ON INTERPOLATION BETWEEN THE ARITHMETIC–GEOMETRIC MEAN AND CAUCHY–SCHWARZ MATRIX NORM INEQUALITIES

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Abstract. In this short note, we obtain an inequality for unitarily invariant norms which is a generalization of one shown by Audenaert [Oper. Matrices. 9 (2015) 475–479]. An application of our result is also given.

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