

INEQUALITIES RELATED TO THE ARITHMETIC, GEOMETRIC AND HARMONIC MEANS

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Abstract. Recent refinements of mean inequalities can be thought of certain ratios. In this article, we present this point of view and prove the relationships between the different ratios induced by the different refinements.

Mathematics subject classification (2010): 15A39, 15B48, 47A63.

Keywords and phrases: Arithmetic means, geometric means, harmonic means, Young's inequality, norm inequalities.

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