

SOME BIVARIATE DURRMEYER OPERATORS BASED ON q -INTEGERS

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Abstract. In the present paper we introduce a q -analogue of the bivariate Durrmeyer operators. A convergence theorem for these operators is established and the rate of convergence in terms of modulus of continuity is determined. Also, a Voronovskaja type theorem has been investigated for these operators.

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