

BOUNDEDNESS ON MORREY SPACE OF MULTILINEAR SINGULAR INTEGRAL OPERATORS SATISFYING A VARIANT OF HÖRMANDER'S CONDITION

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Abstract. We prove the boundedness properties on Morrey space of the multilinear operator associated to the singular integral operator satisfying a variant of Hörmander's condition.

Mathematics subject classification (2010): 42B20, 42B25.

Keywords and phrases: Multilinear operator, singular integral operator, variant of Hörmander's condition, BMO space.

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