

A RECIPROCAL SUM RELATED TO THE RIEMANN ζ -FUNCTION

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Abstract. This paper, we using the elementary method and several new inequalities to study the computational problem of one kind reciprocal sums related to the Riemann zeta-function at the point $s = 4$, and give an explicit computational formula for it.

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