

SOME NEW ITERATED HARDY–TYPE INEQUALITIES AND APPLICATIONS

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Abstract. We characterize some iterated Hardy inequalities previously studied by R. Oinarov and A. Kalybay and, as an application, we give new simpler proofs of the characterizations of the weighted inequalities for the bilinear Hardy operator.

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