

## ON AN ELEMENTARY INEQUALITY AND ITS APPLICATION IN THE THEORY OF INTEGRAL EQUATIONS

JÓZEF BANAŚ AND AGNIESZKA CHLEBOWICZ

*Abstract.* An elementary inequality is proved and some special cases of that inequality are discussed. Moreover, the usefulness of that inequality in the theory of some classes of nonlinear integral equations is shown.

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