

## THE LOG–MINKOWSKI INEQUALITIES FOR QUERMASSTEGRALS

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*Abstract.* Recently, Stancu established the log-Minkowski inequality for non-symmetric convex bodies. In this article, we establish the log-Minkowski inequality for quermassintegrals, which is more general than Stancu's results.

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