

NEW REFINEMENTS OF JENSEN'S INEQUALITY AND ENTROPY UPPER BOUNDS

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Abstract. In this paper some new refinements of the discrete Jensen's inequality with variables are presented. The new refinements are better than the inequalities given by Simic(2009), Dragomir(2010) and Țăpuș, Popescu (2012). As the applications of the refinements, stronger upper bounds for the Shannon's entropy are obtained as well.

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