

## IMPROVEMENTS OF GENERALIZED HÖLDER'S INEQUALITIES AND THEIR APPLICATIONS

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*Abstract.* In this paper, we present some new improvements of generalized Hölder's inequalities, and then we obtain a new refinement of Minkowski inequality. Moreover, the obtained results are used to improve Chung's inequality and Beckenbach-type inequality proposed by Wang.

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