

INEQUALITIES FOR SHEPARD-TYPE OPERATORS

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Abstract. Direct and converse approximation error estimates for generalized Shepard operators are given, improving analogous inequalities for well-known Shepard operators. As application in CAGD, generalized degree elevation algorithms for modeling the shape of Shepard-type curves are presented, improving previous techniques.

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