

## ON WEIGHTED HARDY INEQUALITIES FOR NON-INCREASING SEQUENCES

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*Abstract.* A result of Bennett and Grosse-Erdmann characterizes the weights for which the corresponding weighted Hardy inequality holds on the cone of non-negative, non-increasing sequences and a bound for the best constant is given. In this paper, we improve the bound for  $1 < p \leq 2$ .

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