Journal of Mathematical Inequalities
Volume 12, Number 3 (2018), 677–692
doi:10.7153/jmi-2018-12-52

INEQUALITIES OF THE JENSEN AND EDMUNDSON–LAH–RIBARIČ TYPE FOR 3–CONVEX FUNCTIONS WITH APPLICATIONS

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Abstract. In this paper we derive some Jensen and Edmundson-Lah-Ribarič type inequalities for positive linear functionals and 3-convex functions. Obtained results are then applied to generalized means and power means, as well as to the generalized f-divergence functional. Examples with Zipf-Mandelbrot law are given.

Mathematics subject classification (2010): 26A16, 60E05, 60E15.
Keywords and phrases: Jensen inequality, Edmundson-Lah-Ribarič inequality, 3-convex functions, f-divergence, Zipf-Mandelbrot law.

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Paper JMI-12-52

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