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EXTENDED NORMALIZED JENSEN FUNCTIONAL RELATED TO CONVEXITY, 1–QUASICONVEXITY AND SUPERQUADRACITY

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Abstract. In this paper we extend results related to Normalized Jensen Functional in several directions. We compare a specific Jensen functional with a sum of other functionals for convex functions, and we also extend these results for 1-quasiconvex functions and for Superquadratic functions.

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